



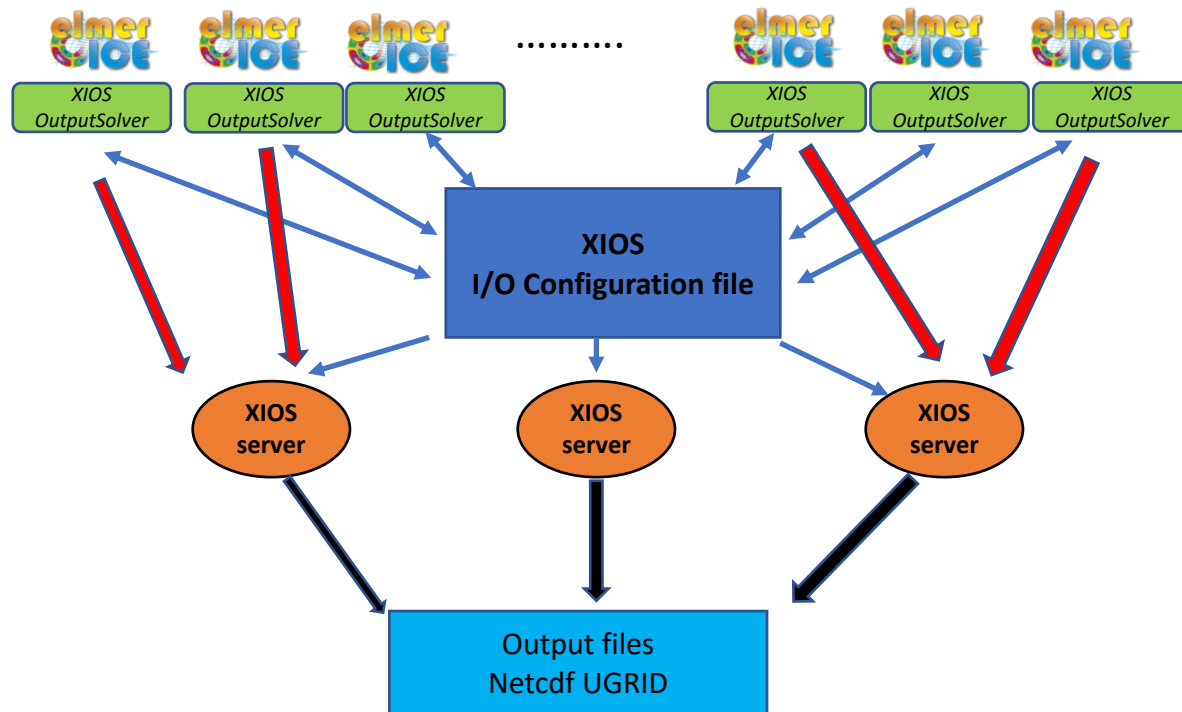
Updates on some Elmer/Ice recent developments

Fabien Gillet-Chaulet

- *I/O with XIOS*
- *(non-linear) Weertman sliding law in **IncompressibleNSVec***
- Spatial covariance modelling

- ***I/O with XIOS***
 - ***Update on the material presented for ElmerIce User meeting in Dec. 2022***
- *(non-linear) Weertman sliding law in IncompressibleNSVec*
- Spatial covariance modelling

- XIOS is a an **external library for I/O** used in several european climate models (e.g. NEMO, LMDz)
- Objectives of XIOS are to address the following challenges for climate data production
 - *Flexibility in management of I/O and data/metadata definition*
 - *Efficient production on supercomputer parallel file systems*
 - *Complexity and efficiency of post-treatment chain to be suitable for distribution and analysis*
- Interface with XIOS as a new Elmer/Ice solver (**XIOSOutputSolver**)
- In detached mode allocate dedicated cpus for XIOS
 - `> mpirun -np XX ElmerSolver_mpi : -np YY xios_server.exe`



- XIOS OutputSolver
 - Update configuration from parameters defined in the .sif
 - Send the grid definition
 - Expose part of the data at each time-step
- XIOS I/O Configuration file
 - Describe the incoming data flow from Elmer/Ice
 - Describe the workflow applied to the incoming data flow:
 - arithmetic filters: $C=A+B$
 - temporal filters : yearly-averaged values
 - spatial filters : sum over the grid, regridding
 - Describe the output files and their content

- SIF file :

```

Solver ....
Exec Solver = After Timestep

Equation = "XIOSOutPutSolve"
Procedure = "ElmerIceSolvers" "XIOSOutputSolver"

....
Keywords related to time unit system, time step, start date
...

! node and elem vars; e.g.
Scalar Field 1 = String "h"
Scalar Field 1 compute cell average = Logical True

Scalar Field 2 = String "acabf "

! Global Variables
Global Variable 1 = String "time"

End
    
```

- XIOS xml config file :

```

<context id="elmerice">
  <!-- calendar -->
  <calendar type="NoLeap" time_origin="1995-01-01 00:00:00" />

  <!-- fields -->
  <field_definition>

    <field id="h" standard_name="land_ice_thickness" unit="m" grid_ref="GridNodes" operation="instant" />
    <field id="h_elem" standard_name="land_ice_thickness" unit="m" grid_ref="GridCells" operation="instant" />

    <field id="acabf" standard_name="land_ice_surface_specific_mass_balance_flux" unit="m d-1" grid_ref="GridCells" operation="average" />

    <field id="time" name="elmer_time" unit="d" grid_ref="ScalarGrid_sum" operation="instant" />

    <field id="ismip6_acabf" field_ref="acabf" name="acabf" unit="kg m-2 s-1" > this*$rhoi/$nsec_per_day </field>

  </field_definition>

  <!-- files -->
  <file_definition >

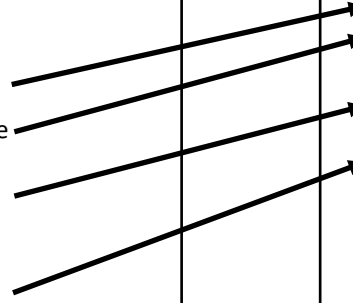
    <file_group id="file01" >
      <file id="file01" name="MyFileName" convention="UGRID" output_freq="1y" >
        <field field_ref="ismip6_acabf" />
        <variable id="elmerversion" name="model_version" type="string"> elmer ice </variable>
      </file>

    </file_group >

  </file_definition >

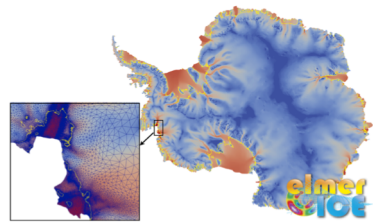
  ...

</context>
    
```



Codes, tools, files to run and process standard ISMIP6 simulations maintained by IGE:

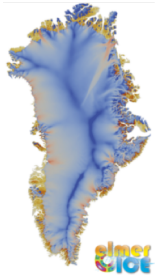
- https://github.com/pmathiot/ELMER_ISMIP6_Antarctica



ISMIP6-Antarctica-2300:

- 2 contributions:
 - IGE; J. Caillet
 - UTAS; C. Zhao
- **SSA** (shelves, 1km-50km)
- I/O-Post-Processing; Melt parameterisations

- https://gricad-gitlab.univ-grenoble-alpes.fr/gilletcf/elmerice_ismip6_gris



ISMIP6-compliant:

- IGE; F. Gillet-Chaulet
- CSC; T. Zwinger
- **SSA** (shelves)
- I/O-Post-Processing; Forced Front Retreat



• Outputs in netcdf UGRID

- contain meta-data
- Restartable (independent of number of partitions) => *UGridDataReader*
- Viewable
 - QGIS : as mesh layer with the Crayfish plugin
 - **Paraview: reader under development => download a recent nightly build**
- Can use many functionalities to manipulate netcdfs nco, cdo....
 - e.g. ncdiff => differences between netcdfs => compare simulations, anomalies
 - E.g. ncea => ensemble average
- **Temporal filters**
 - Compute time averaged values (or min, max , cumulative)
- **Calendar management**
- **Used/developped by relatively large community in climate models**



- **Restricted to 2D => 2D boundary of a 3D vertically extruded Mesh**
- **Configuration**
 - Need to read *XIOS* documentation and tutorials
- **Works with geographical coordinates (lon,lat)**
 - Module *ProjUtils* : (lon/lat) <=> (x,y)
 - Analytical implementation for polar stereographic north (Greenland) and south (Antarctica)
 - **Interface with fortran gis and proj4 for other projections (UTM)**
 - *To see what to do for synthetic experiments...*
- **Calendar management**
 - a year is not a proper time unit (duration depends on the calendar)
 - Time step should be an integer value and a given fraction of the output frequency

> *ncdump output_file.nc*

```

dimensions:
  axis_nbounds = 2 ;
  Two = 2 ;
  nmesh2D_node = 221562 ;
  nmesh2D_edge = 633466 ;
  nmesh2D_face = 411985 ;
  nmesh2D_vertex = 3 ;
  time = UNLIMITED ; // (86 currently)
variables:
  int mesh2D ;
      mesh2D:cf_role = "mesh_topology" ;
      mesh2D:long_name = "Topology data of 2D unstructured mesh" ;
      mesh2D:topology_dimension = 2 ;
      mesh2D:node_coordinates = "mesh2D_node_x mesh2D_node_y" ;
      mesh2D:edge_coordinates = "mesh2D_edge_x mesh2D_edge_y" ;
      mesh2D:edge_node_connectivity = "mesh2D_edge_nodes" ;
      mesh2D:face_edge_connectivity = "mesh2D_face_edges" ;
      mesh2D:edge_face_connectivity = "mesh2D_edge_face_links" ;
      mesh2D:face_face_connectivity = "mesh2D_face_links" ;
      mesh2D:face_coordinates = "mesh2D_face_x mesh2D_face_y" ;
      mesh2D:face_node_connectivity = "mesh2D_face_nodes" ;
  float mesh2D_node_x(nmesh2D_node) ;
      mesh2D_node_x:standard_name = "longitude" ;
      mesh2D_node_x:long_name = "Longitude of mesh nodes." ;
      mesh2D_node_x:units = "degrees_east" ;
  float mesh2D_node_y(nmesh2D_node) ;
      mesh2D_node_y:standard_name = "latitude" ;
      mesh2D_node_y:long_name = "Latitude of mesh nodes." ;
      mesh2D_node_y:units = "degrees_north" ;

  double time(time) ;
      time:axis = "T" ;
      time:standard_name = "time" ;
      time:long_name = "Time axis" ;
      time:calendar = "noleap" ;
      time:units = "days since 1995-01-01 00:00:00" ;
      time:time_origin = "1995-01-01 00:00:00" ;
      time:bounds = "time_bounds" ;
  double time_bounds(time, axis_nbounds) ;

  float xvelmean(time, nmesh2D_face) ;
      xvelmean:standard_name = "land_ice_vertical_mean_x_velocity" ;
      xvelmean:units = "m s-1" ;
      xvelmean:mesh = "mesh2D" ;
      xvelmean:location = "face" ;
      xvelmean:online_operation = "instant" ;
      xvelmean:interval_operation = "1 yr" ;
      xvelmean:interval_write = "1 yr" ;
      xvelmean:cell_methods = "time: point" ;
      xvelmean:_FillValue = 1.e+20f ;
      xvelmean:missing_value = 1.e+20f ;
      xvelmean:coordinates = "time_instant mesh2D_face_y mesh2D_face_x" ;

// global attributes:
  :name = "ismip6_states_marv3.12_access1.3-rcp85-rhigh_1" ;
  :description = "Created by xios" ;
  :title = "Created by xios" ;
  :Conventions = "UGRID" ;
  :timeStamp = "2022-Nov-09 05:54:35 GMT" ;
  :uuid = "49aa435f-f62d-4b8e-81d3-0191d3ea4f75" ;
  :model_version = "Elmer/Ice v9.0 (Rev: 29fd3bf4)" ;
  :altitude_convention = "altitude reference against geoid EIGEN-EC4" ;
  :projection = "espg:3413" ;

```

- *(non-linear) Weertman sliding law in **IncompressibleNSVec***
- *I/O with XIOS*
- *Spatial covariance modelling*

- Implemented a long time ago by Peter
- Previously prescribed as a USF: **Sliding_Weertman** in USF_Sliding.f90
- **Latest elmerice branch (762e8f2db – March 1st 2023)**
 - Implement **Newton method** for non-linear iterations
 - Shows expected speed-up in the **convergence of non-linear iterations**
 - Examples:
 - elmerice/Tests/Friction_WeertmanNewton2/
 - elmerice/Tests/Friction_WeertmanNewton3D
 - To see for GL applications where contact is tested inside the non-linear iterations loop
 - Update the **adjoint inverse method** to invert for the friction coefficient
 - No proof that it should be better than inverting for the effective friction, but might introduce a discontinuity between inversion and transient simulations
 - Examples:
 - elmerice/examples/Inverse_Methods/StokesWeertman
 - **Need to update the doc.**
 - Implement Coulomb-type friction law (Newton and inversion)?

```
Boundary Condition 5
  Name = "bottom"
  Body Id = 3

  !! Normal-Tangential coordinate system
  Normal-Tangential Velocity = Logical True
  Velocity 1 = Real 0.0

  Weertman Friction Coefficient = Variable alpha
  REAL procedure "ElmerIceUSF" "TenPowerA"
  Weertman Exponent = Real 0.33333333333333333333
  ! Cut-off such that argument is not smaller than this
  Friction Linear Velocity = Real 1.0e-4

  Slip Coefficient derivative = Variable alpha
  REAL procedure "ElmerIceUSF" "TenPowerA_d"

  Bottom Surface = Variable Coordinate 1
  Real MATC "-tx*tan(Slope)-1000.0"
End
```

- (non-linear) Weertman sliding law in `IncompressibleNSVec`
- I/O with XIOS

- **Spatial covariance modelling**

- ***Come to see my PICO about regularisation in the Mass conservation method***

CR2.3 **EDI** ✨

Beyond the unconstrained: Driving and assisting cryospheric models with observations | PICO ▶

Co-organized by CL5/GI5/HS13

Convener: Elisa Mantelli^{ECS} Q | Co-conveners: Johannes Sutter Q, Nanna Bjørnholt Karlsson Q, Olaf Eisen Q

▶ PICO ★ | **Fri, 28 Apr, 10:45–12:30 (CEST)** ■ PICO spot 3a

- **Codes in elmerice branch since Jan. 2023 (ef1e0b1f1)**

- elmerice/Solvers/Covarianceutils:

- **BackgroundErrorCostSolver.F90** => Data Assimilation (Regularisation)
- **GaussianSimulationSolver.F90** => Generate random fields from the given covariance matrix
- **CovarianceVectorMultiplySolver.F90** => Gaussian Filter

- **No documentation, no automatic testing and no examples yet in the distribution; just ask if interested...**

Inverse methods from a Bayesian perspective: the linear gaussian case

We consider the following inverse problem:

Estimate the « true » state of a system $\mathbf{x}^t \in \mathbb{R}^n$, from a set of observations $\mathbf{y}^o \in \mathbb{R}^m$ (in general $m \ll n$), such that:

$$\mathbf{y}^o = \mathbf{H}\mathbf{x}^t + \epsilon^o$$

\mathbf{H} is a linear **observation operator**
 ϵ^o is the observation error (assumed unbiased), with **covariance matrix** \mathbf{R}

We also have a first estimate \mathbf{x}^b (from lab experiments, a climatology, a previous model forecast, ...), such that :

$$\mathbf{x}^b = \mathbf{x}^t + \epsilon^b$$

ϵ^b is the **background error** (assumed unbiased), with **covariance matrix** \mathbf{B}

The Best Linear Unbiased Estimation (BLUE) is given by :

$$\mathbf{x}^a = \mathbf{x}^b + \mathbf{K} (\mathbf{y}^o - \mathbf{H}\mathbf{x}^b) \quad \text{where the Kalman gain is given by } \mathbf{K} = \mathbf{B}\mathbf{H}^T (\mathbf{R} + \mathbf{H}\mathbf{B}\mathbf{H}^T)^{-1}$$

After some calculations, it can be shown that **the same estimation minimises** the following **cost function**:

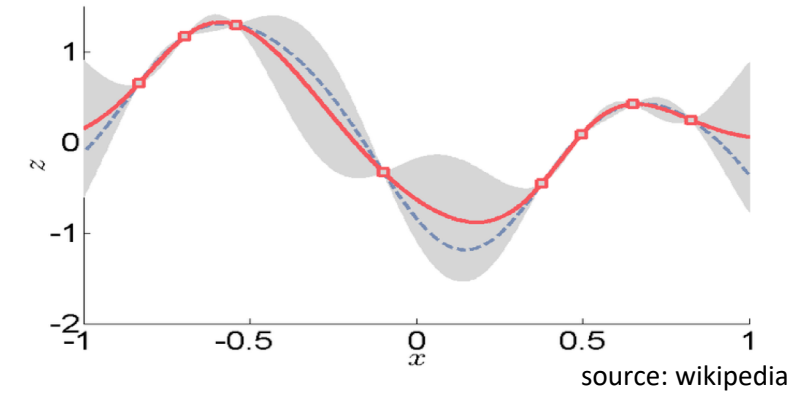
$$J(\mathbf{x}) = \frac{1}{2}(\mathbf{y}^o - \mathbf{H}\mathbf{x})\mathbf{R}^{-1}(\mathbf{y}^o - \mathbf{H}\mathbf{x}) + \frac{1}{2}(\mathbf{x} - \mathbf{x}^b)\mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}^b) \quad \Rightarrow \text{Can be seen as a "Regularisation" term}$$

Comments:

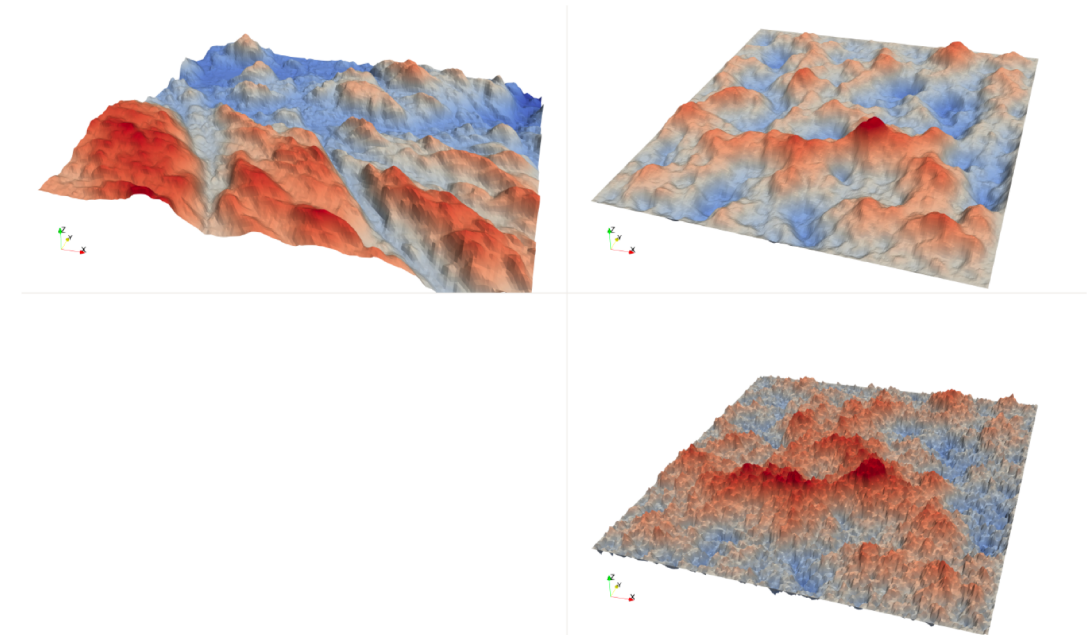
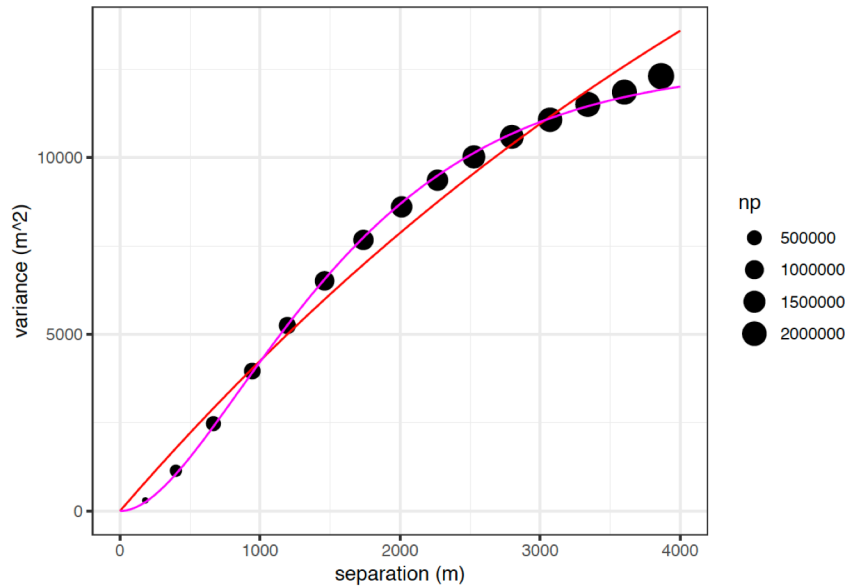
- => Require to properly define the covariance matrices \mathbf{R} and \mathbf{B} (and the background)
- => "scientific issues" for properties that are very poorly constrained (friction)
- => "technical issues" covariances matrices are full-rank matrices so in general you can not store them
- => in general no proof of optimality for non-linear, non-gaussian, biased cases

Scientific issues:

- Analogies with geostatistic:
 - Interpolation by **Kriging** requires to parametrized prior co-variances using standard correlation functions (Exponential, Gaussian, Matérn, ...)



Correlation function (variograms)



Rq. in general real bed elevations are not gaussian, there is features (valleys, ..)

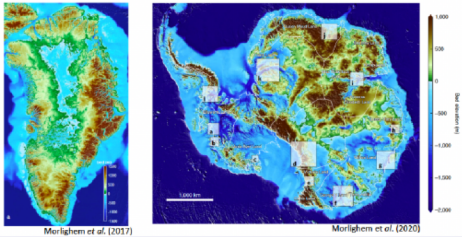
Scientific issues:

- Analogies with geostatistic:
 - Interpolation by **Kriging** requires to parametrized prior co-variances using standard correlation functions (Exponential, Gaussian, Matérn, ...)

Numerical issues:

- You don't really need B, but an equivalent **operator** (the action of B on a vector)
 - **Diffusion operators** can be used to model a class of correlation functions from the Matérn family (cf e.g. Guillet et al., 2019)
 - It consist in iteratively solving a diffusion-type equation
 - => can be applied on unstructured meshes with the FEM
 - => relatively cheap and memory efficient
- I have implemented the possibility to compute B (and B-1 and L)
 - with **standard correlation functions** (and lapack routines to compute the inverse and square root)
 - => restricted to **small serial problems** (~up to 10-20 knodes)
 - **with the diffusion operator approach** (based on Guillet et al. 2019)
 - => **can be used for large parallel simulations**

The mass conservation method



- is a method to interpolate radar-derived ice thickness data
- is used in the reference **BedMachine** products

=> is in Elmer/Ice since a while but has never really been used

is a control method

- The ice thickness, H , is solution of the **steady-state** continuity equation:

$$\nabla(\bar{\mathbf{u}}H) = \dot{a}$$

- The optimal ice thickness H minimizes:

$$J(\bar{\mathbf{u}}, \dot{a}) = \frac{1}{2}(H - H^{obs})\mathbf{R}^{-1}(H - H^{obs}) + \frac{1}{2}R_{reg}$$

Objective: Test the sensitivity to the regularisation term R_{reg}

- is often chosen as a **Tikhonov** regularisation term that penalizes spatial derivatives of H :

$$R_T(H) = \lambda \int_{\Omega} \|\nabla H\|^2 d\Omega$$

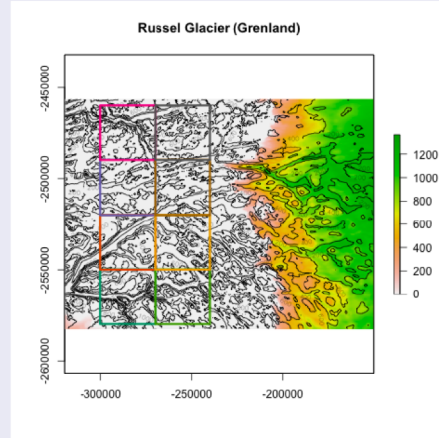
- In a **Bayesian** framework, regularisation is introduced from prior information about the solution:

$$R_B(H) = (H - H^b)\mathbf{B}^{-1}(H - H^b)$$

Synthetic twin experiments

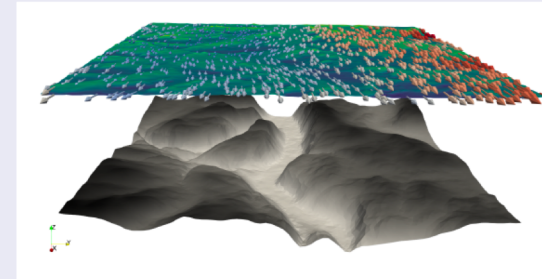
1. Take deglaciated beds

8 test cases: 30×30 km boxes



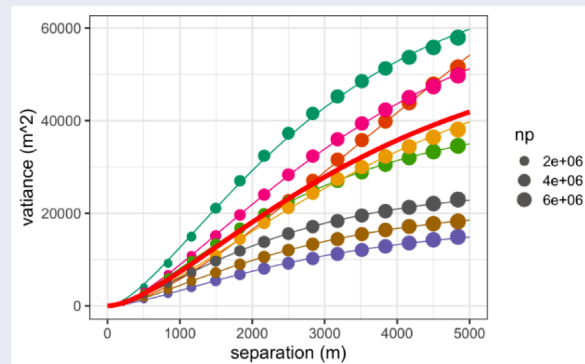
2. Add 1000 m of ice

Generate a perfect model solution



3. Regularisation $R_B(H)$

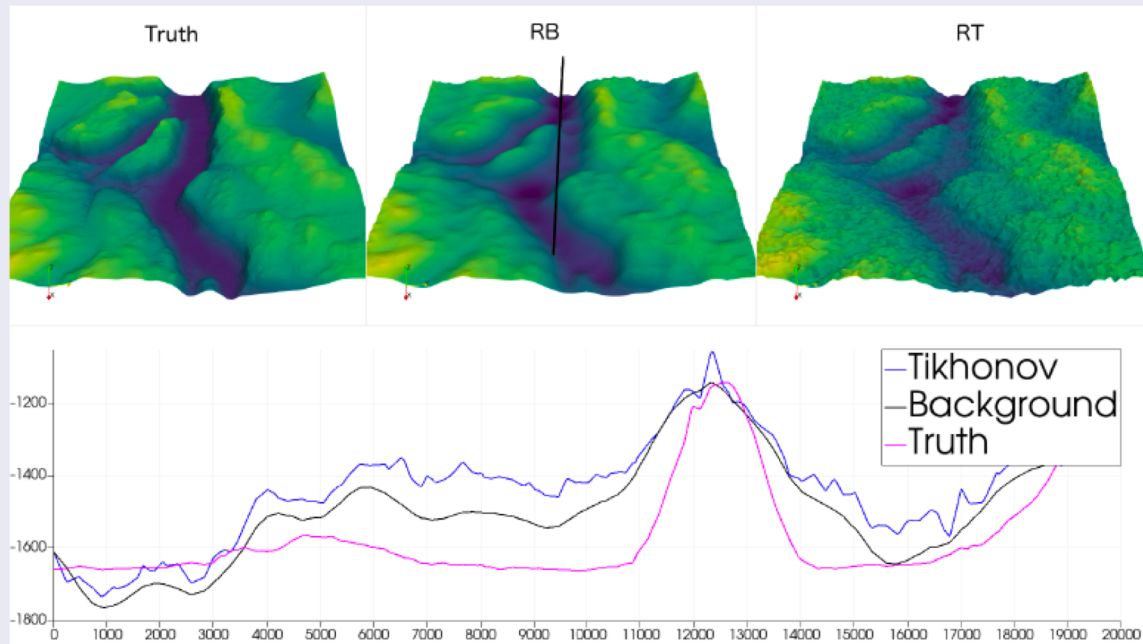
Parameterize B^{-1}



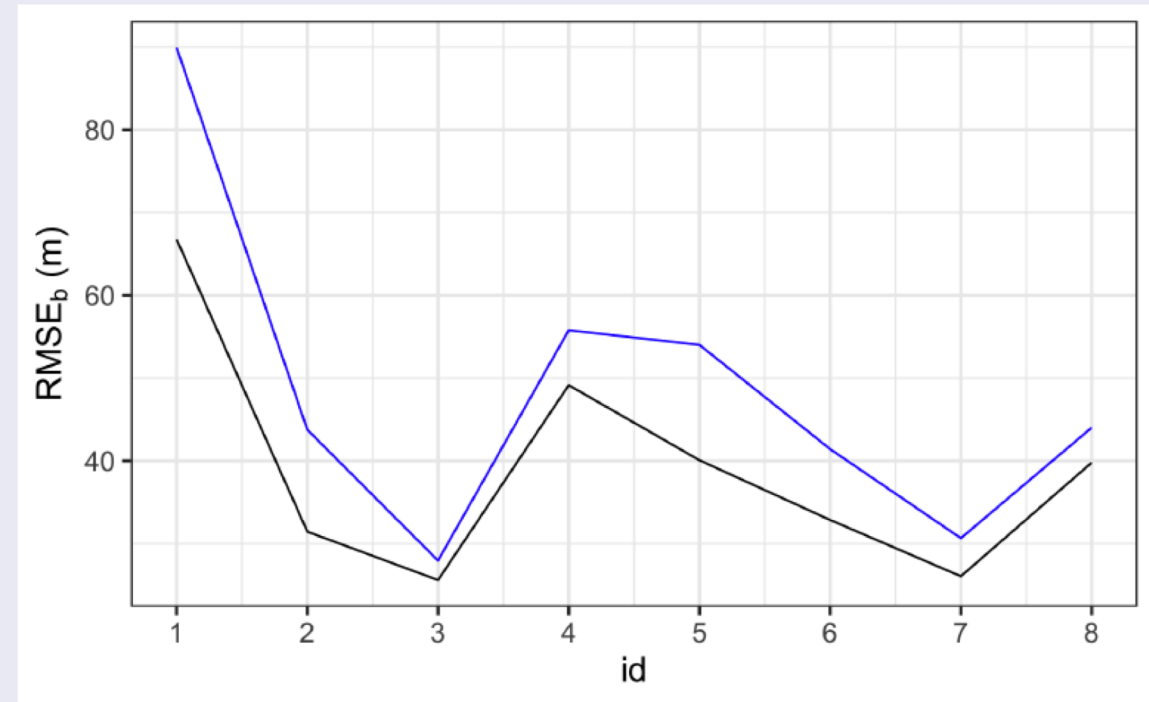
- **spatial correlation** is parametrised using standard correlation functions, as done for kriging
- Fit standard **Matérn covariance** functions from variograms using geostatistical modelling tools
- B^{-1} is applied as a diffusion operator on the unstructured FE mesh (Guillet et al., 2019)

Results

Reconstructed beds (id=1)

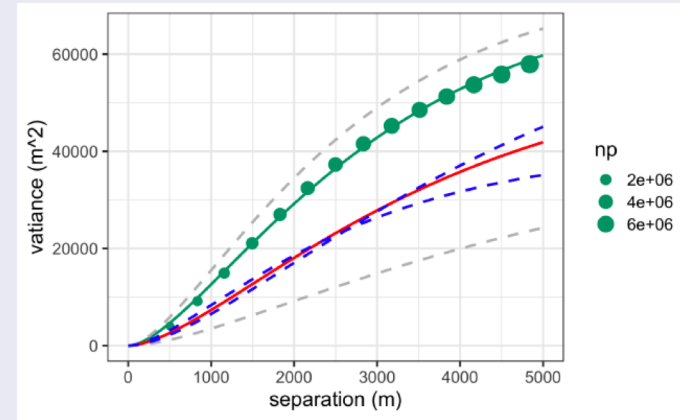
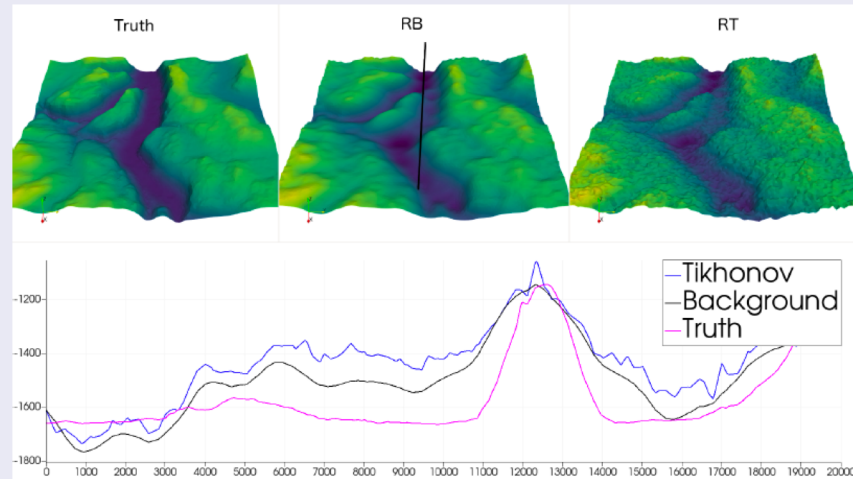


RMSE_b for all cases

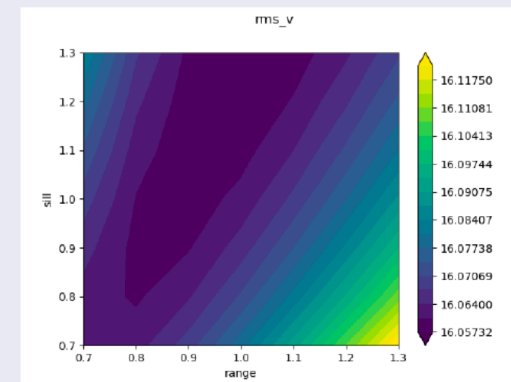
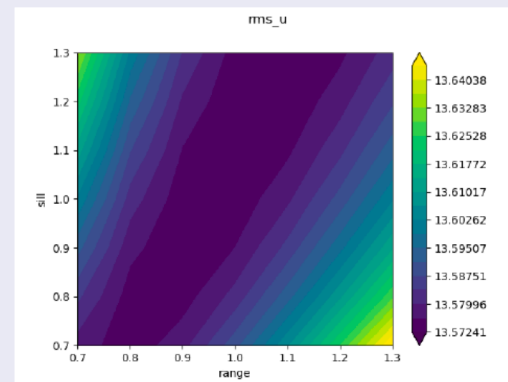
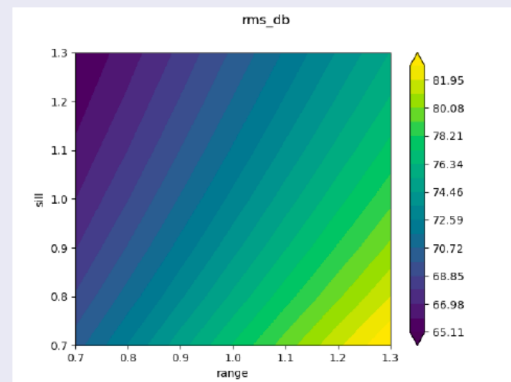


- $R_B(H)$ regularisation **always provides the best reconstruction**
- $R_T(H)$ underestimates correlation at short distances

Results: Case 1



- Sensitivity to range and sill:



Possible applications with these tools:

- **Data assimilation (B^{-1}) => BackgroundErrorCostSolver.F90**
 - More difficult to define B for friction/viscosity inversions
 - But not so different that adjusting the weights in Tikhonov regularisation and you can show that it's equivalent in some cases (regular 1D mesh, ...)
 - Parameters (range; sill) have physical meanings and should be consistent across mesh resolution
 - See e.g. A framework for time-dependent Ice Sheet Uncertainty Quantification, applied to three West Antarctic ice streams, Recinos et al., under review (TCD) and presented by J. Maddison in the modelling session
- **Gaussian simulations ($B=LL^T$; $y=\mu + L.z$) => GaussianSimulationSolver.F90**
 - You can **draw random samples** using the same parameterised covariance matrix (requires to compute the square root)
 - **Uncertainty quantification using ensemble methods**
 - See Bulthuis, K., & Larour, E. (2022). Implementation of a Gaussian Markov random field sampler for forward uncertainty quantification in the Ice-sheet and Sea-level System Model v4.19. *Geoscientific Model Development*, 15(3), 1195–1217.
<https://doi.org/10.5194/gmd-15-1195-2022>
- **Gaussian filters (smoothing noisy data) (B) => CovarianceVectorMultiplySolver.F90**

