

Simulating Antarctic subglacial hydrology processes beneath Pine Island Glacier, using GlaDS in Elmer/Ice

yufang zhang

John Moore^{1 2} Mike Wolovick¹ Rupert Gladstone²
Thomas Zinger³ Xiaoran Guo¹

Ice dynamics, basal hydrology, Antarctica, GlaDS, Elmer/ice, PIG

Why important to study (simulate) subglacial hydrology system?

- Subglacial drainage system influences basal sliding
- Contribute to SLR and have an impact on SLR prediction
- Previous work on ice dynamics involves little hydrology feedback
- Difficult to directly observe sub-environment
- Couple hydrology model to ice dynamics may give more specific SLR

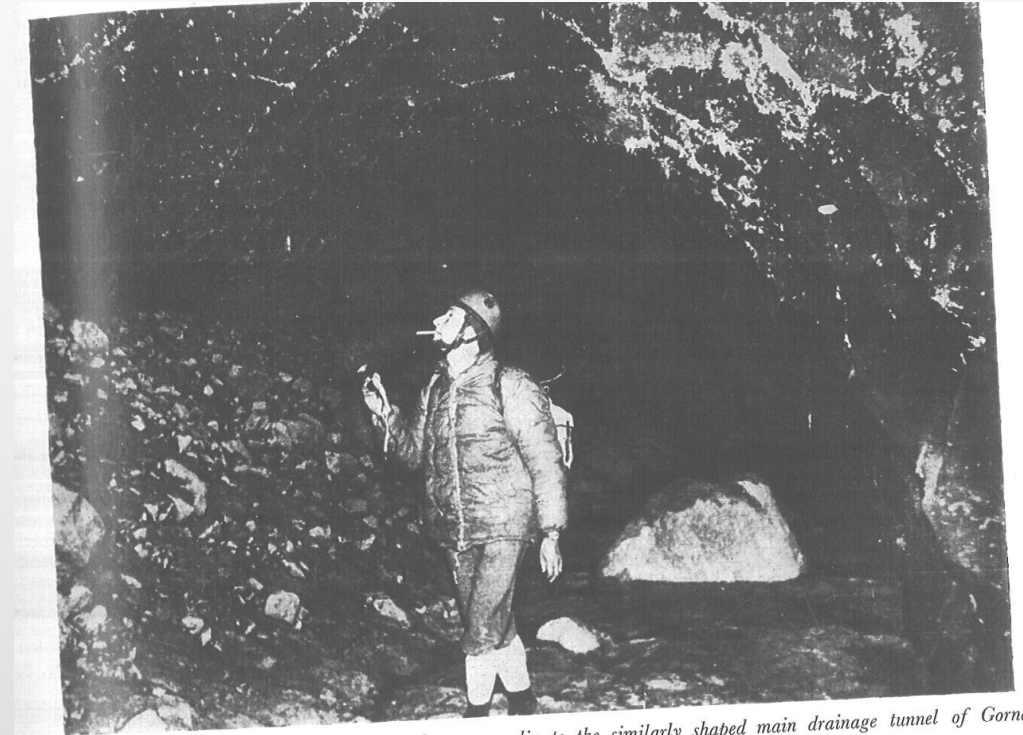


Fig. 11. Typical section of the duct leading from a moulin to the similarly shaped main drainage tunnel of Gornersee. (Photograph by Luc Vuadens, Groupe St. Exupéry).

Hydrology model developments

- Conduit model (Rothlisberger et al., 1972)
- Box model (Clarke et al., 1996)
- Flow-line model (Flowers et al., 2004)
- 2D network model (Schoof et al., 2012; Shugar et al., 2017)
- GlaDS, coupled distributed and continuous drainage model (Werder et al., 2013; Dow et al., 2016; Dow et al., 2020)

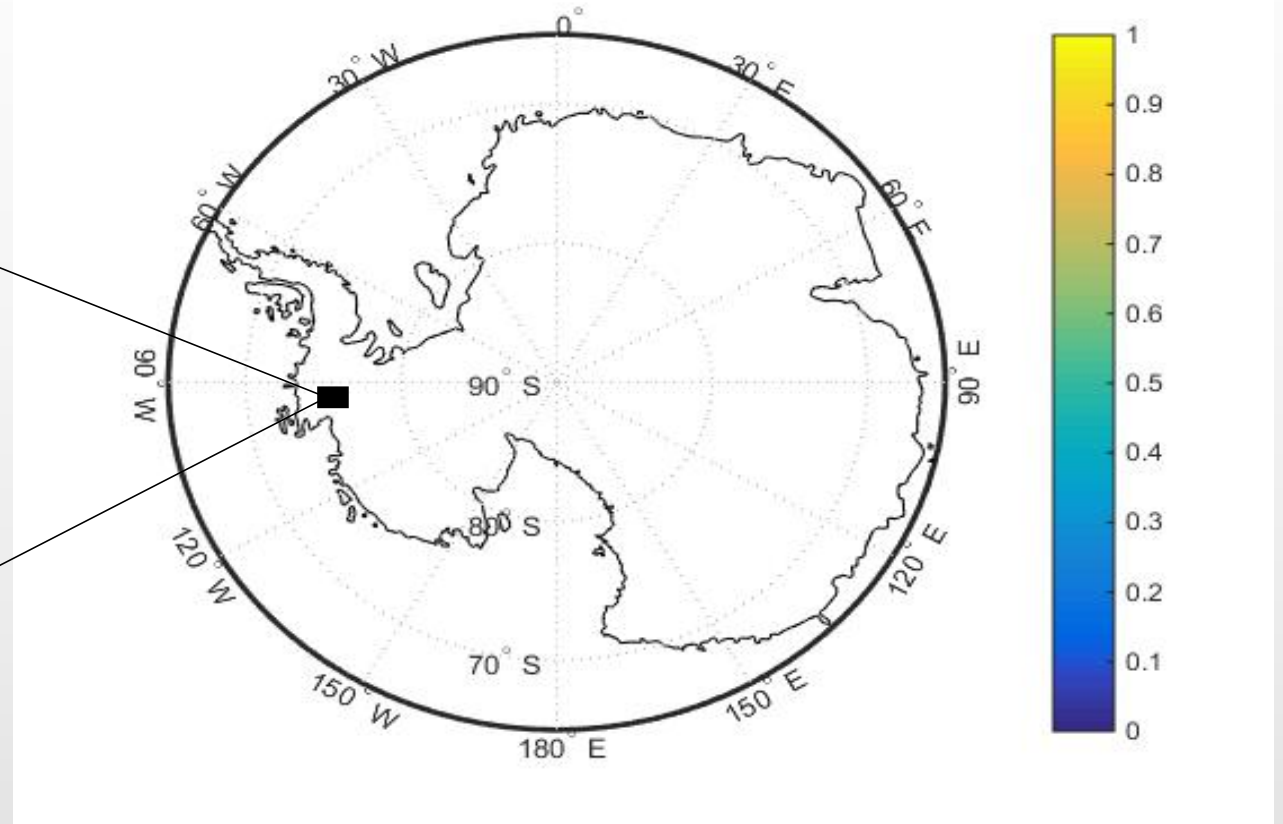
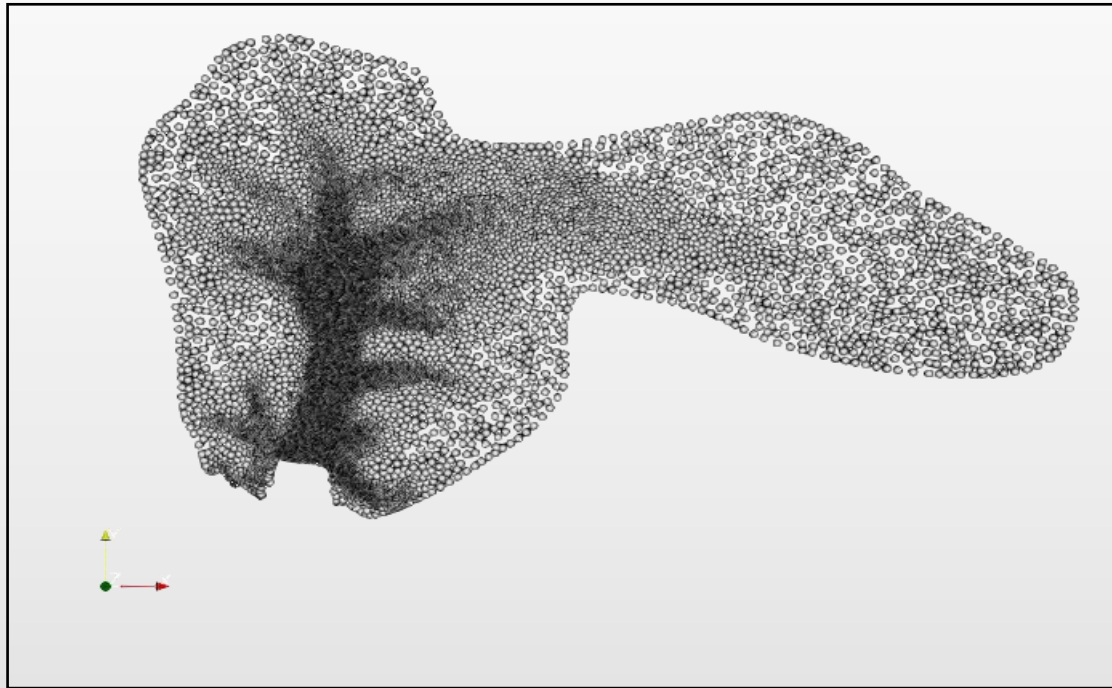
GlaDS model in Elmer/Ice

- Oliver Gagliardini, Mauro A. Werder., 2018
- de Fleurian et al., SHMIP project, 2017

My research work focus on applying [GlaDS in Elmer/Ice to a marine-terminating glacier](#), Pine Island Glacier, West Antarctica, to reveal realistic hydrology system and test centurial timescale evolution under climate scenarios.

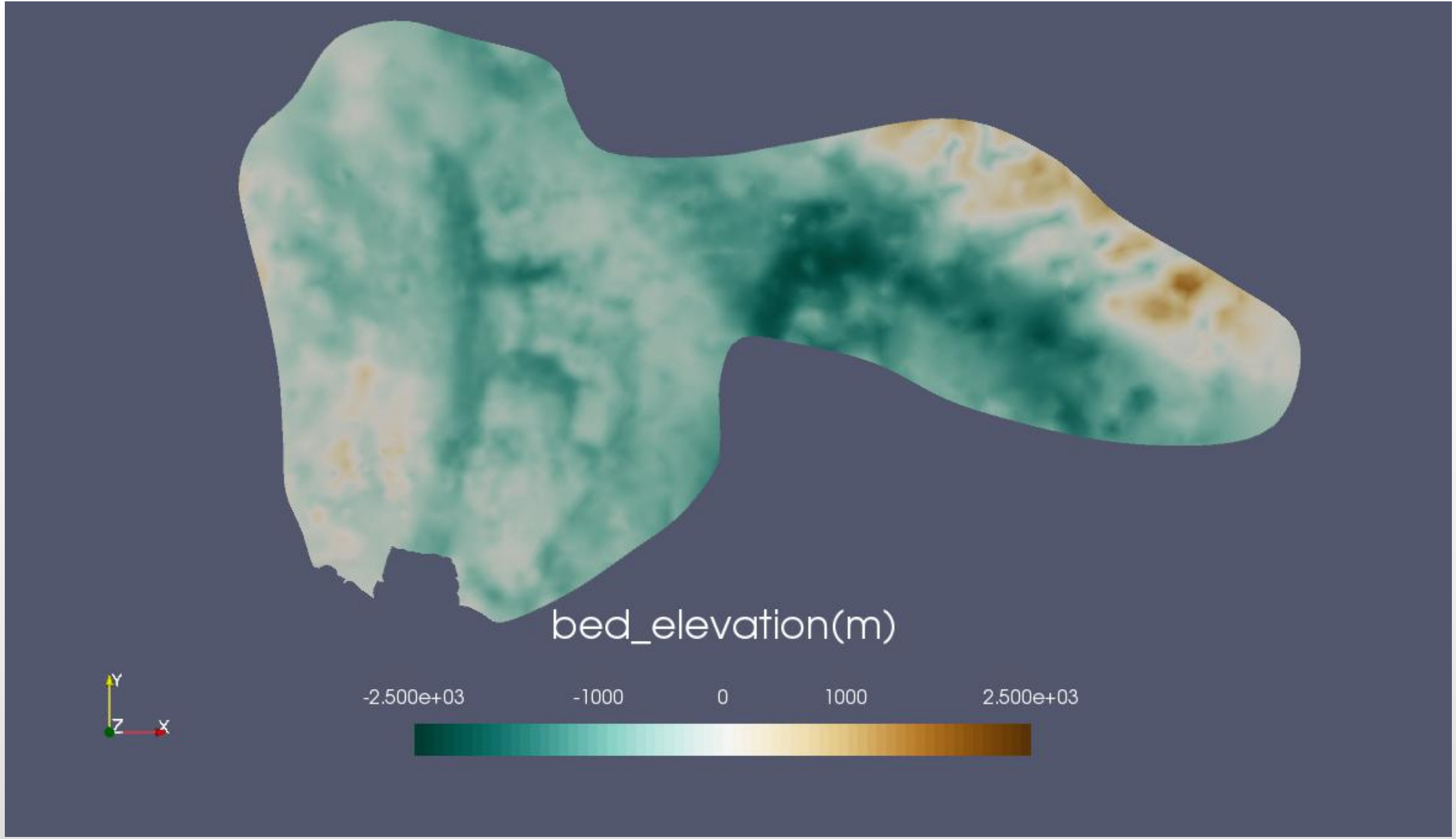
Reason of choosing Pine Island Glacier, West Antarctica

- One of the biggest mass loss and contribution to SLR.
- One of the fastest retreated glacier, 4000 m s⁻¹



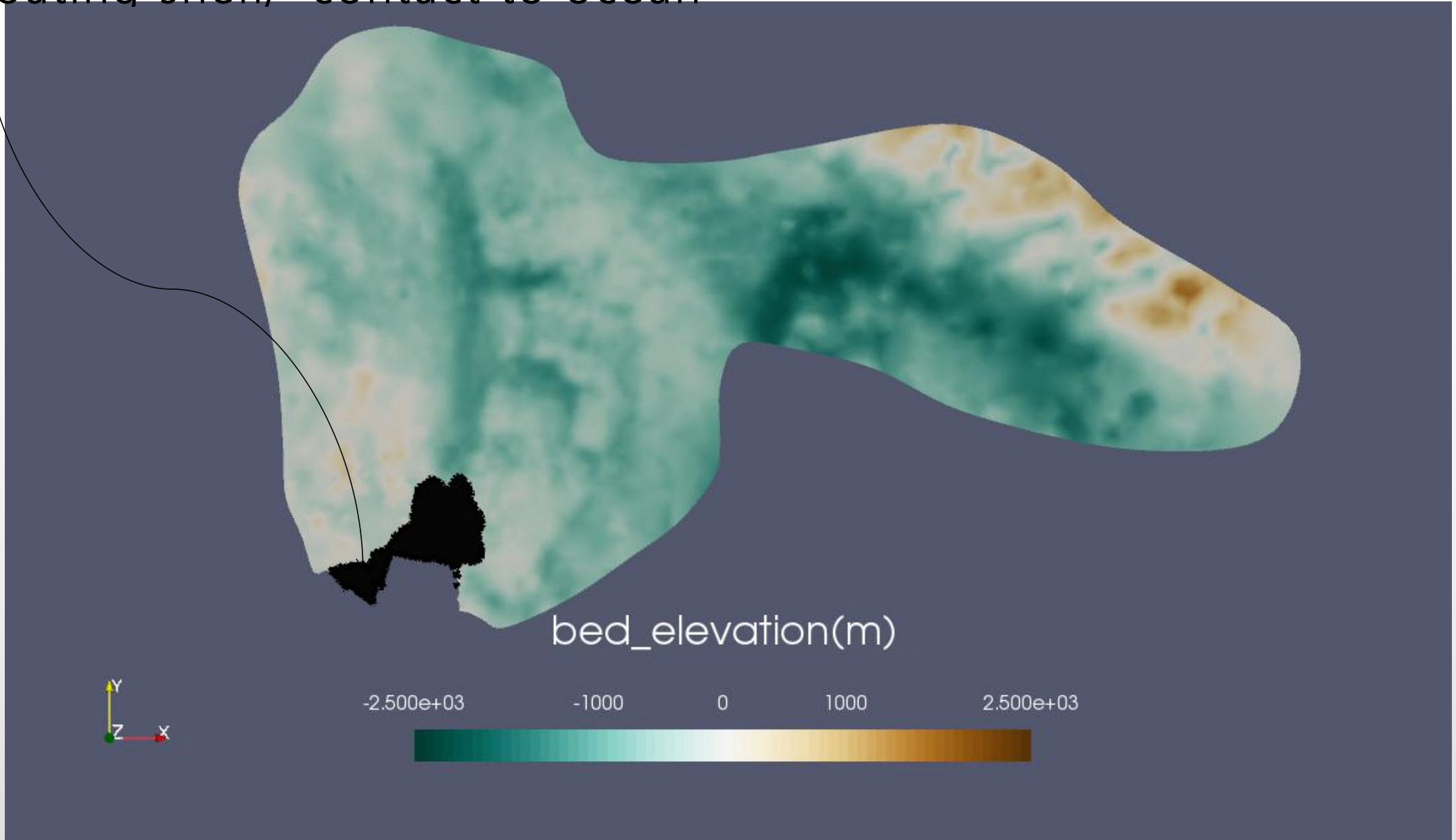
Domain & Topography

trough in the center of PIG



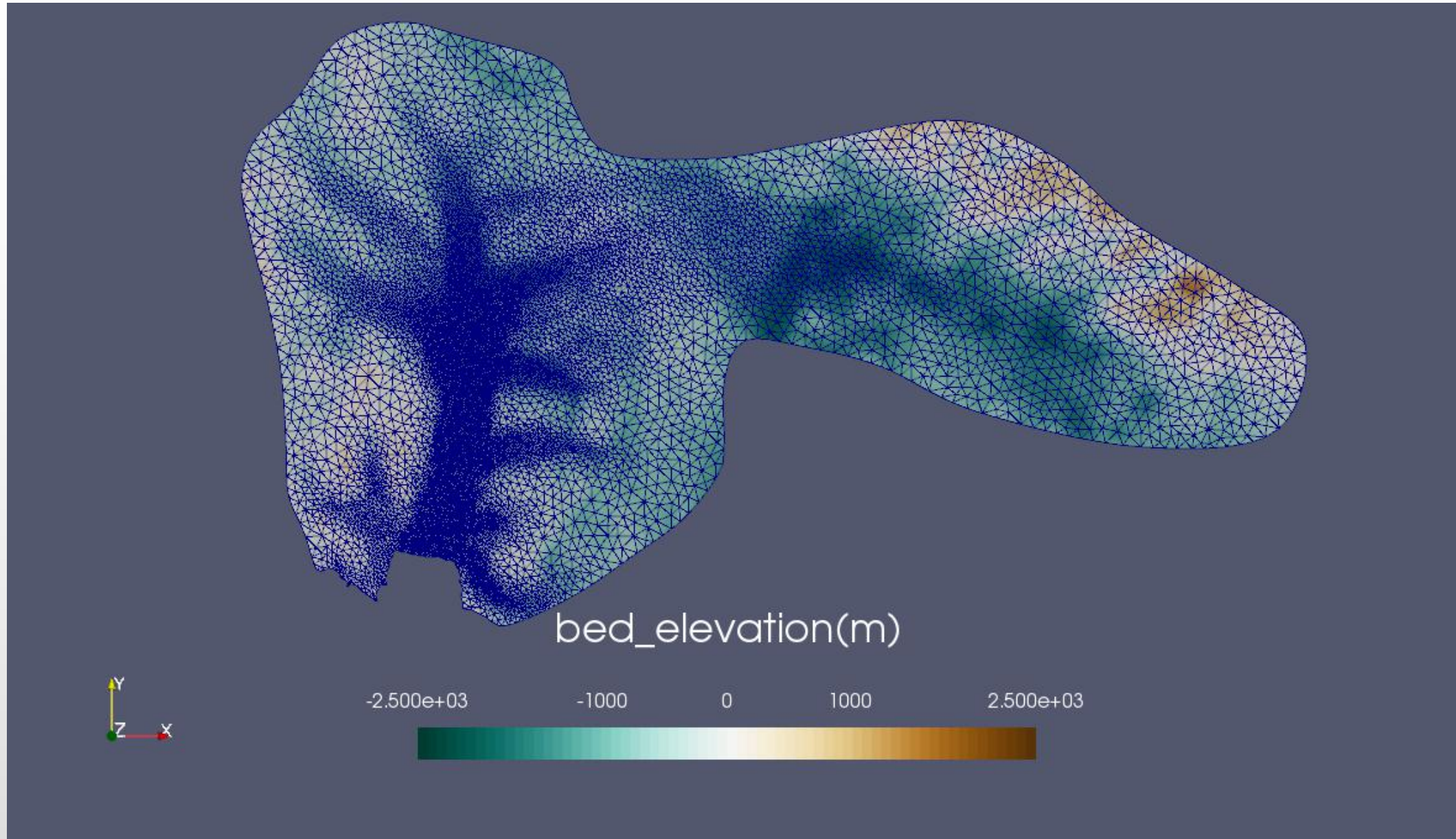
Domain & Topography

ice floating shelf, contact to ocean



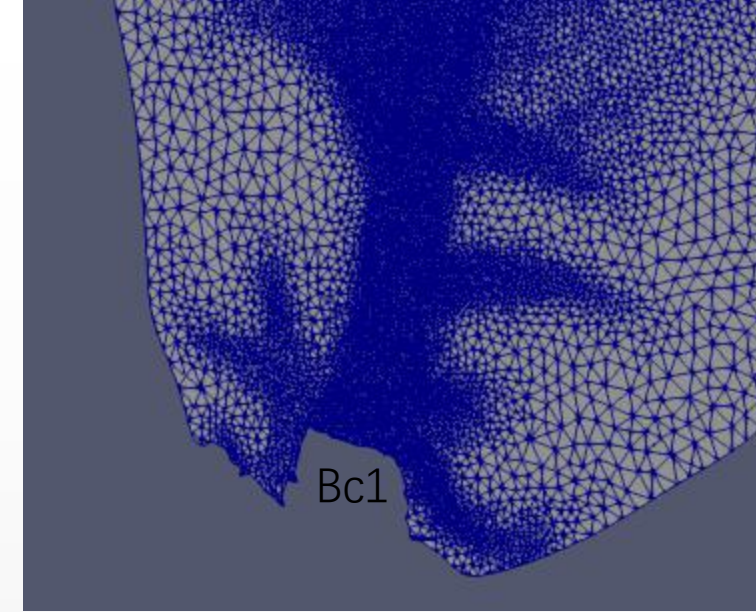
Unstructured triangle mesh; Different density

from Rupert Gladstone.



Bodys and Boundary Condition

- including 3 bodys, one shared body
- BC, set on lower surface, inland
- Direchelet BC: $HP, N, Pw = 0$
- Run 2000 days (over 4 years), output every 50 days
- waterinput1: Constant Water Input = $0.01m a^{-1}$



Bc 1 is floating line boundary .

Water Input 2 from inversion model

Parameters

parameters and equations controls hydrology process

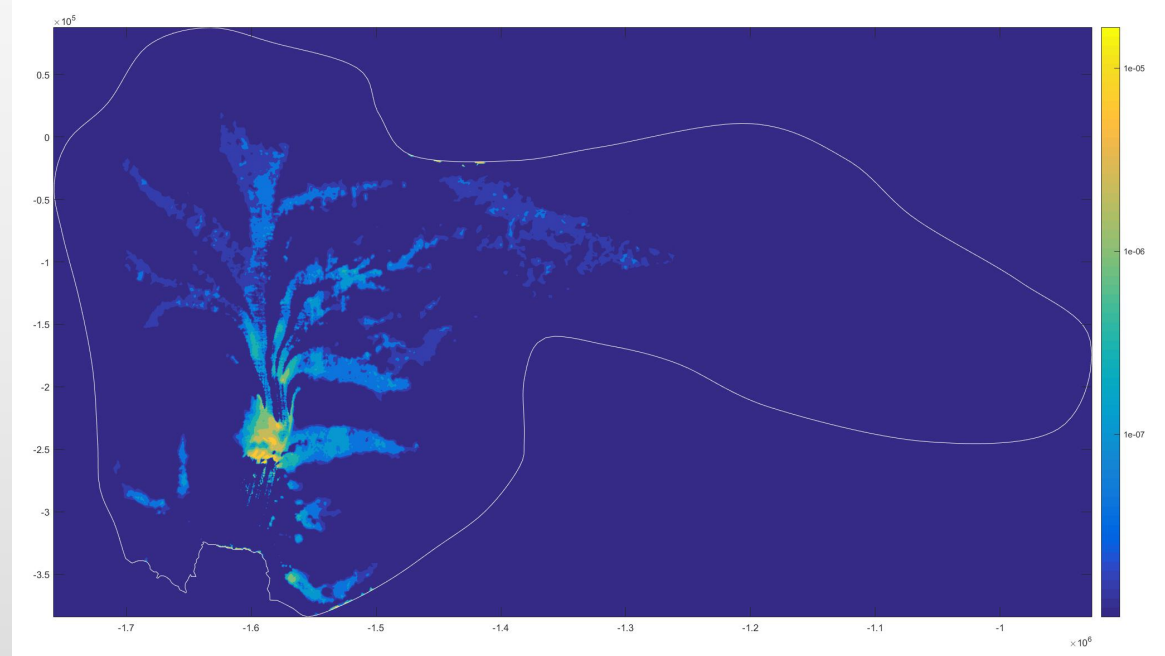
Table 1. Parameters and Values Used in Synthetic Model Runs^a

Description	Symbol	Value	Units
Acceleration due to gravity	g	9.81	$m s^{-2}$
Latent heat	L	3.34×10^5	$J kg^{-1}$
Ice density	ρ_i	910	$kg m^{-3}$
Water density	ρ_w	1000	$kg m^{-3}$
Pressure melt coefficient	c_i	7.5×10^{-8}	$K Pa^{-1}$
Heat capacity of water	c_w	4.22×10^3	$J kg^{-1} K^{-1}$
First sheet flow exponent	α	5/4	
Second sheet flow exponent	β	3/2	
First channel flow exponent	α_c	5/4	
Second channel flow exponent	β_c	3/2	
Sheet conductivity ^b	k	0.01	$m^{7/4} kg^{-1/2}$
Channel conductivity ^c	k_c	0.1	$m^{3/2} kg^{-1/2}$
Glen's n	n	3	
Ice flow constant cavities	\bar{A}	5×10^{-25}	$Pa^m s^{-1}$
Ice flow constant channels	\bar{A}_c	5×10^{-25}	$Pa^m s^{-1}$
Basal sliding speed	u_b	10^{-6}	$m s^{-1}$
Sheet width below channel ^d	l_c	2	m
Cavity spacing	l_r	2	m
Bedrock bump height	h_r	0.1	m
Englacial void ratio	e_c	10^{-3}	
Moulin cross-sectional area	A_m	10	m^2
Bed elevation	B		m
Ice thickness	H		m
Sheet input	m		$m s^{-1}$
Moulin input	Q_c		$m^3 s^{-1}$

Table 2. Variables and Units^a

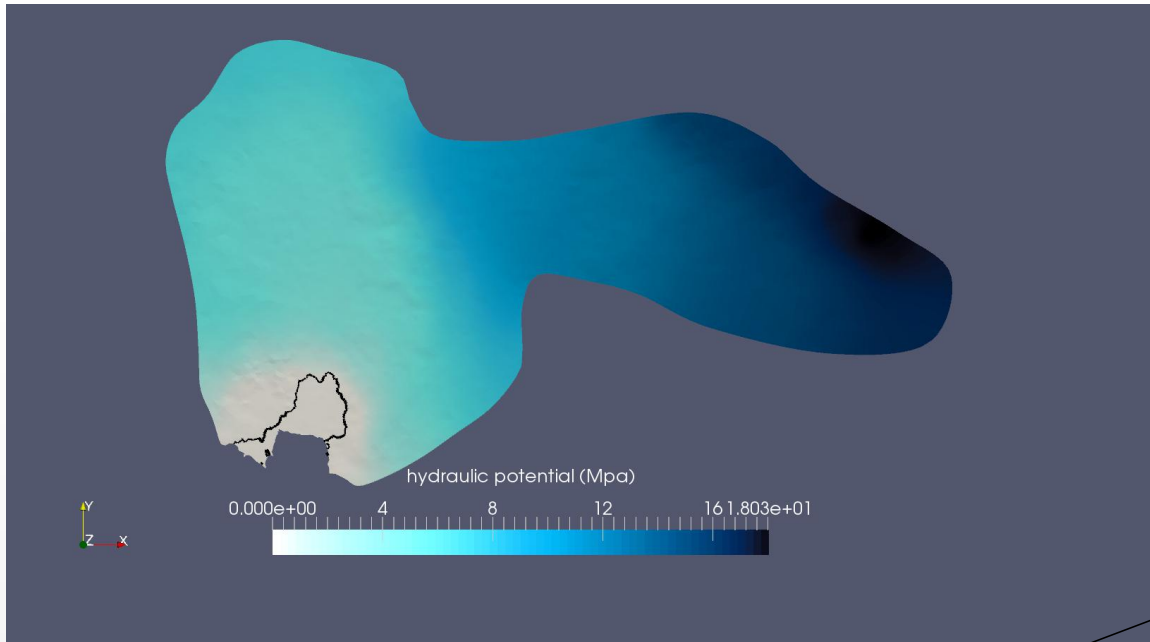
Description	Variable	Units
Hydraulic potential	ϕ	Pa
Channel discharge	Q	$m^3 s^{-1}$
Channel cross-sectional area	S	m^2
Sheet discharge	q	$m^2 s^{-1}$
Sheet thickness	h	m
Time coordinate	t	s
Along edge coordinate	s	m
Normal vector	n	m
Test function	θ	Pa
Englacial storage	h_e	m
Hydraulic potential of bed	ϕ_m	Pa
Overburden hydraulic potential	ϕ_0	Pa
Effective pressure	N	Pa
Cavity opening rate	w	$m s^{-1}$
Cavity closure rate	v	$m s^{-1}$
Channel dissipation	Π	$W m^{-1}$
Channel press-melt	Ξ	$W m^{-1}$
Channel closure rate	v_c	$m^2 s^{-1}$
Sheet flow beneath channel	q_c	$m^2 s^{-1}$
Water volume in moulin	V_m	m^3

outputs: hydraulic potential, ice discharge, effective pressure

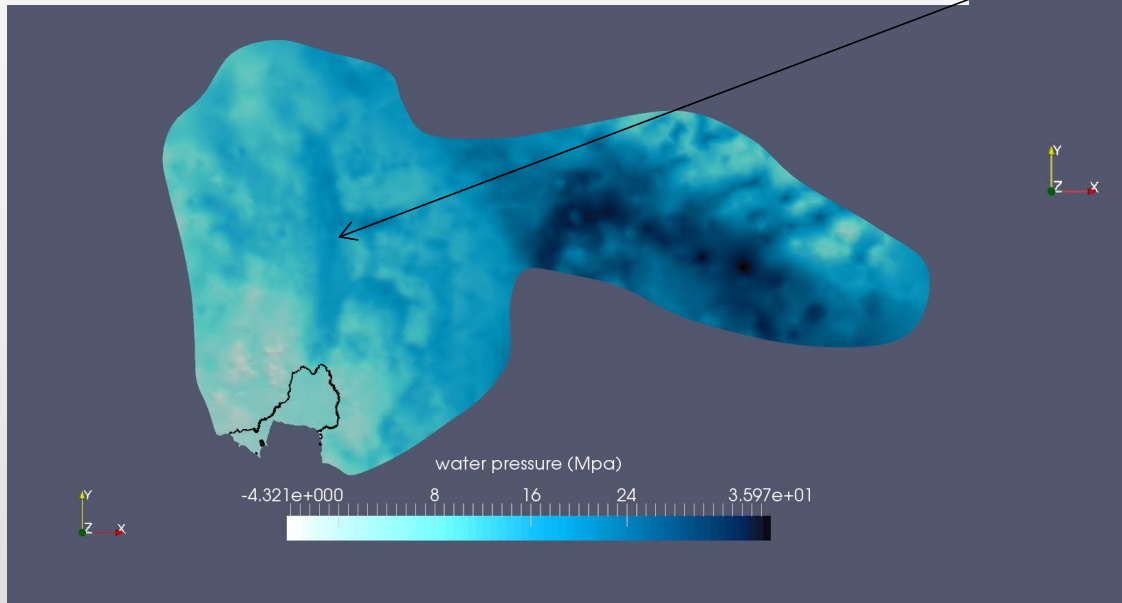


Results 800days

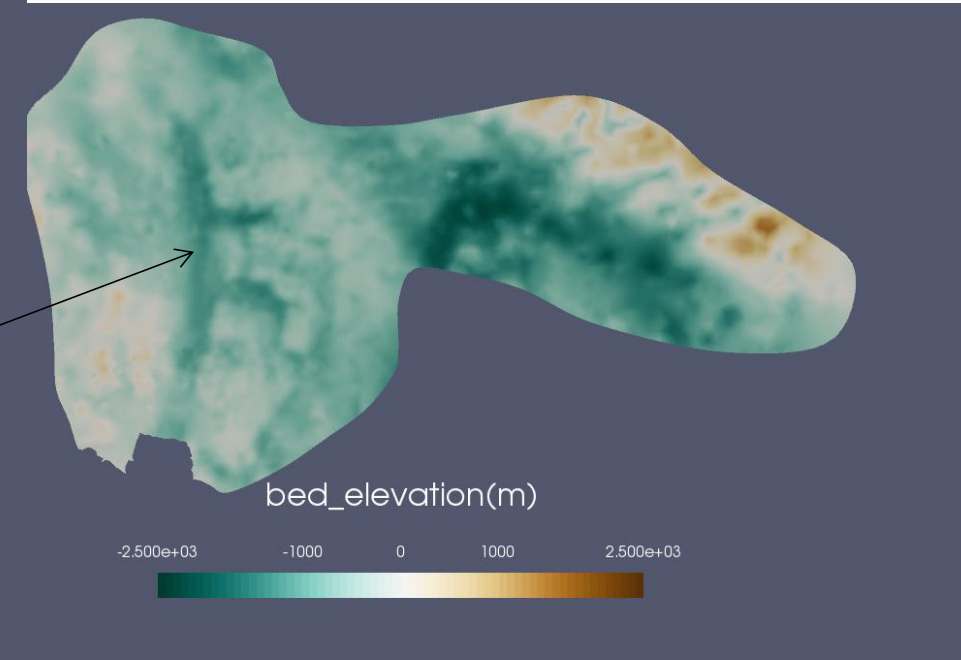
Hydraulic potential



Water Pressure

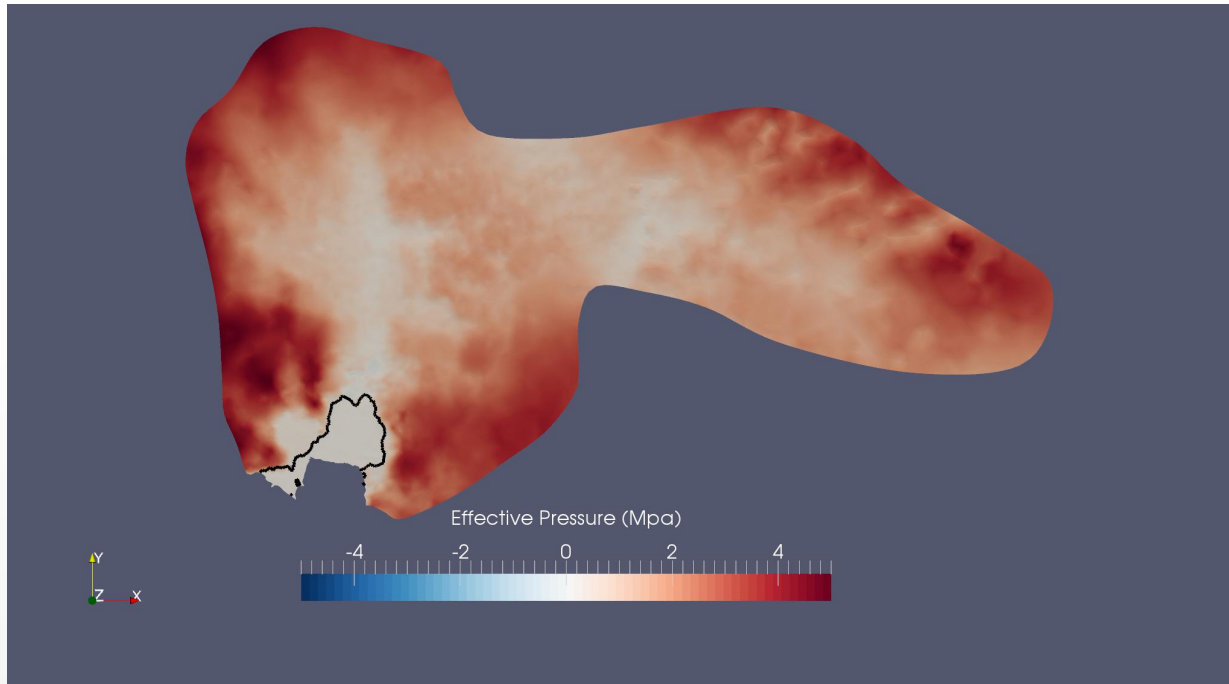


- When water pressure increases, the gradient of hydraulic potential increases.
- Strong correspondence in regions of faster sliding velocity with high water pressure. (along the troughs)



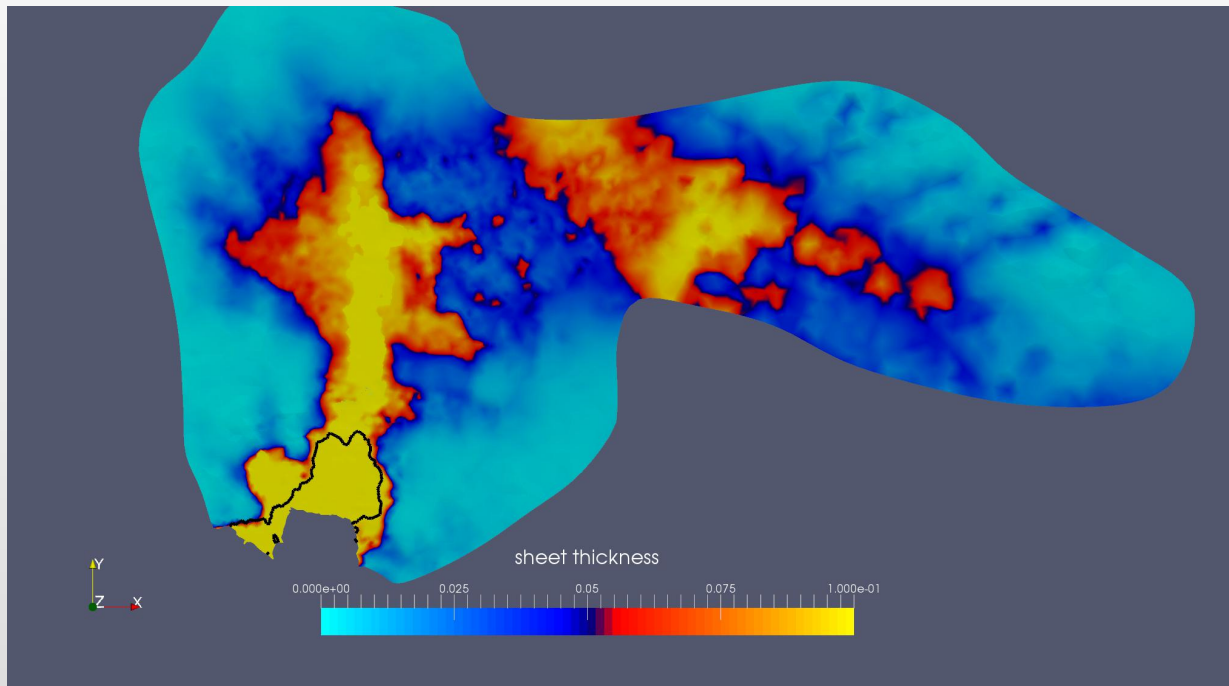
Results 800days

Effective Pressure



- Agreement of high water pressure with presence of sheet thickness.
- Water pressure is basically the same with ice overburden pressure.

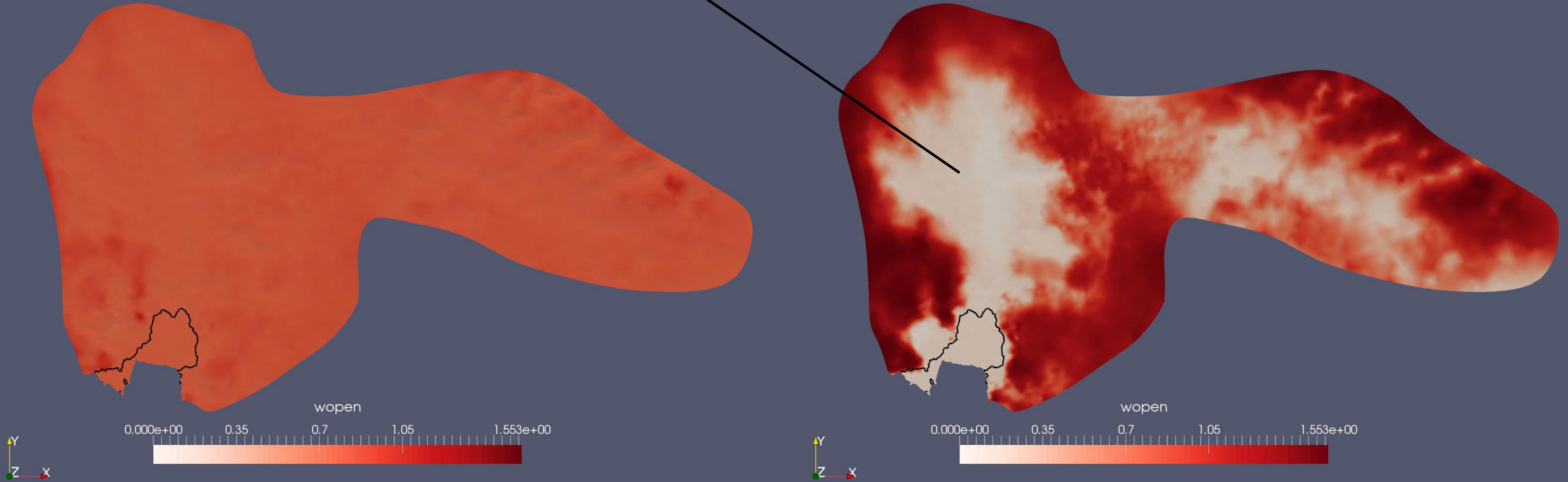
Sheet thickness



Results

cavity opening rate

$$w(h) = \begin{cases} \frac{u_b (h_r - h)}{l_r}, & h < h_r \\ 0, & \text{otherwise} \end{cases} \quad \begin{matrix} h_r = 0.1(\text{m}) & l_r = 2(\text{m}) \\ \text{sheet thickness is bigger than height of bed bump.} \end{matrix}$$



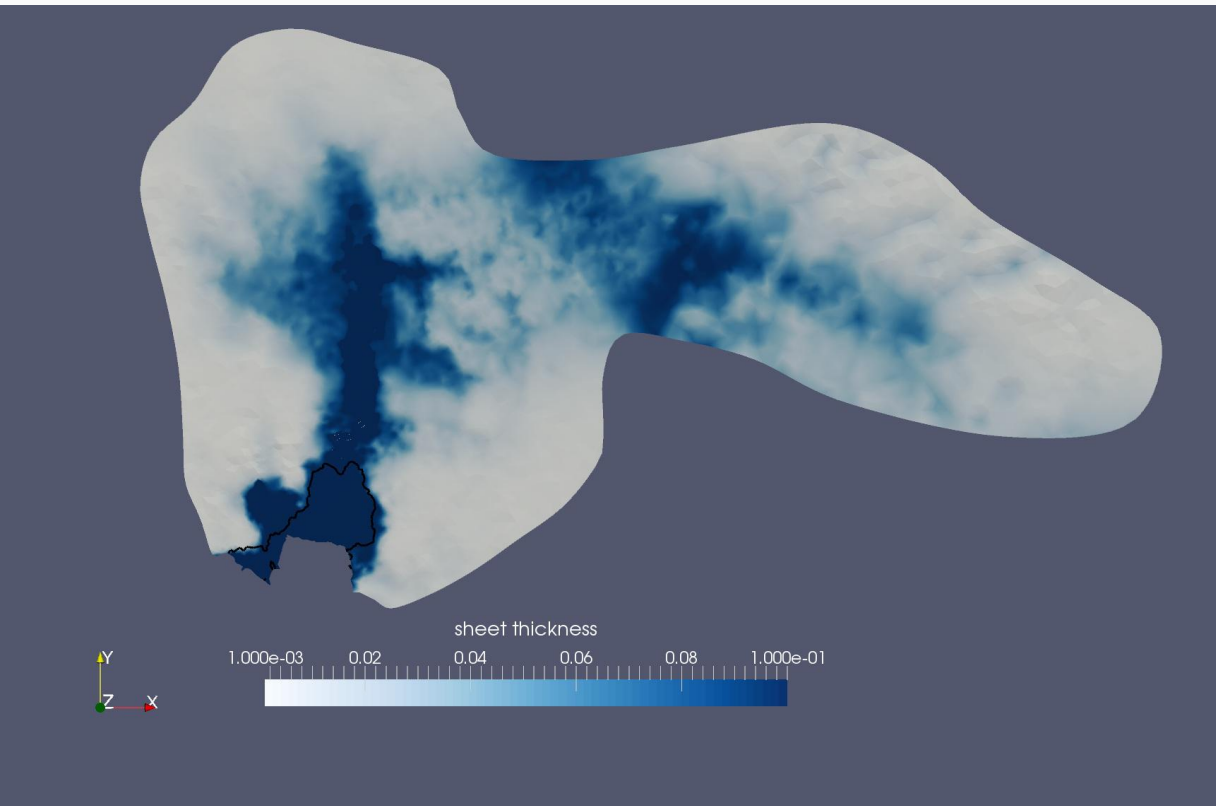
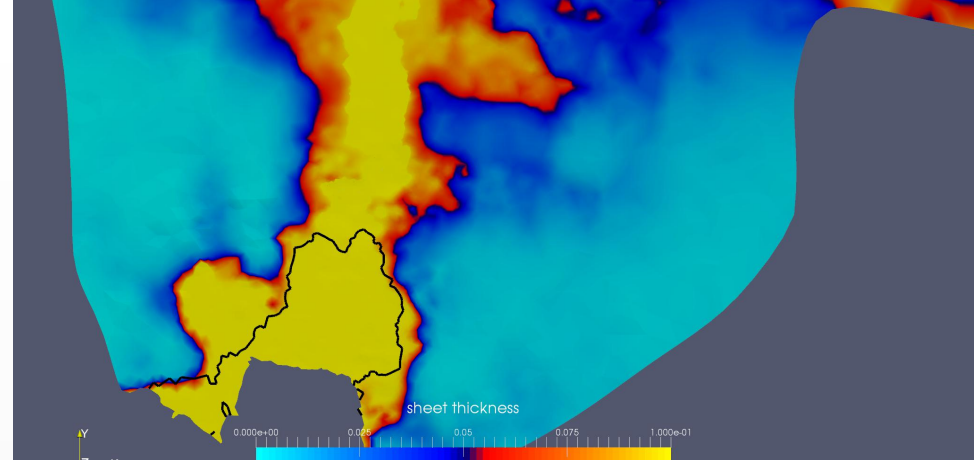
water input 1

Results

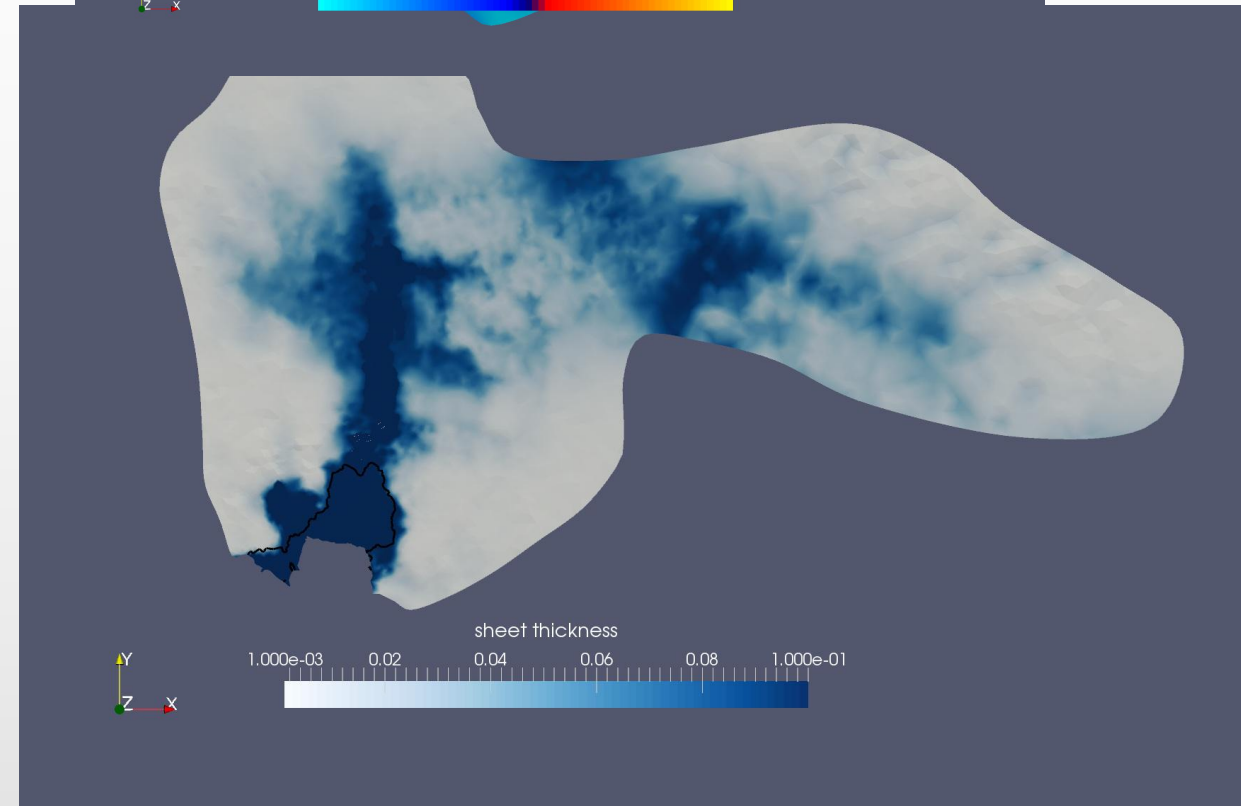
Sheet thickness

h [0.001,0.1] m

$$\frac{\partial h}{\partial t} = w - v$$

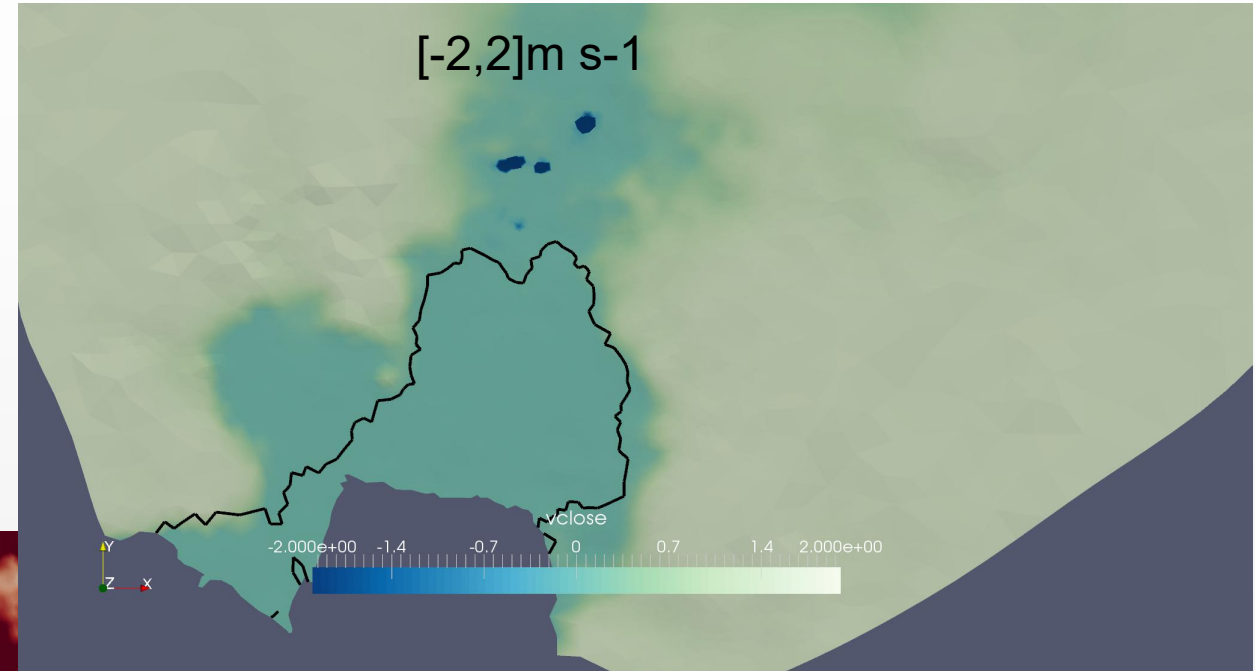
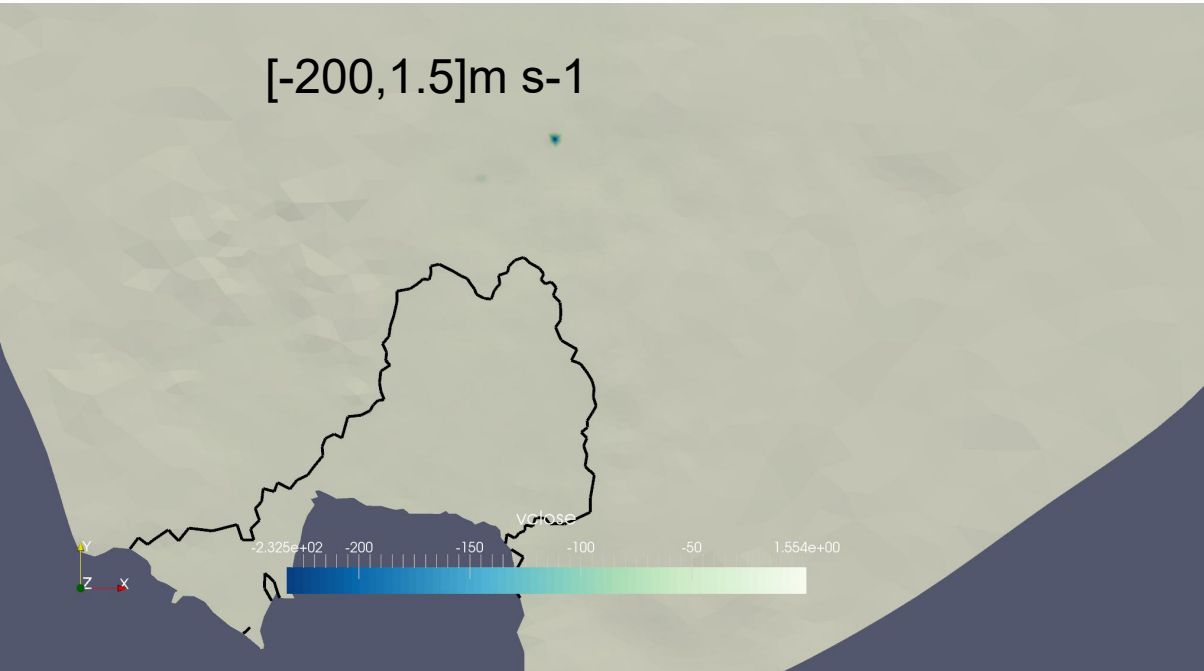


800days

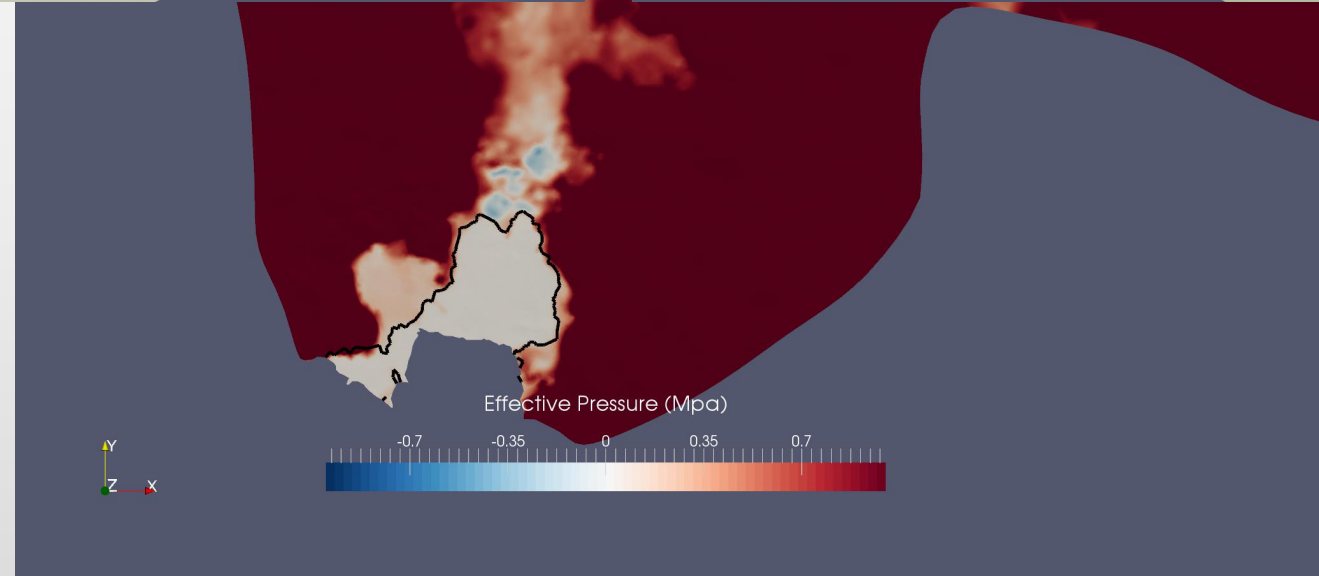


850days

$$v(h, N) = Ah|N|^{n-1}N$$



not reasonable due to water input



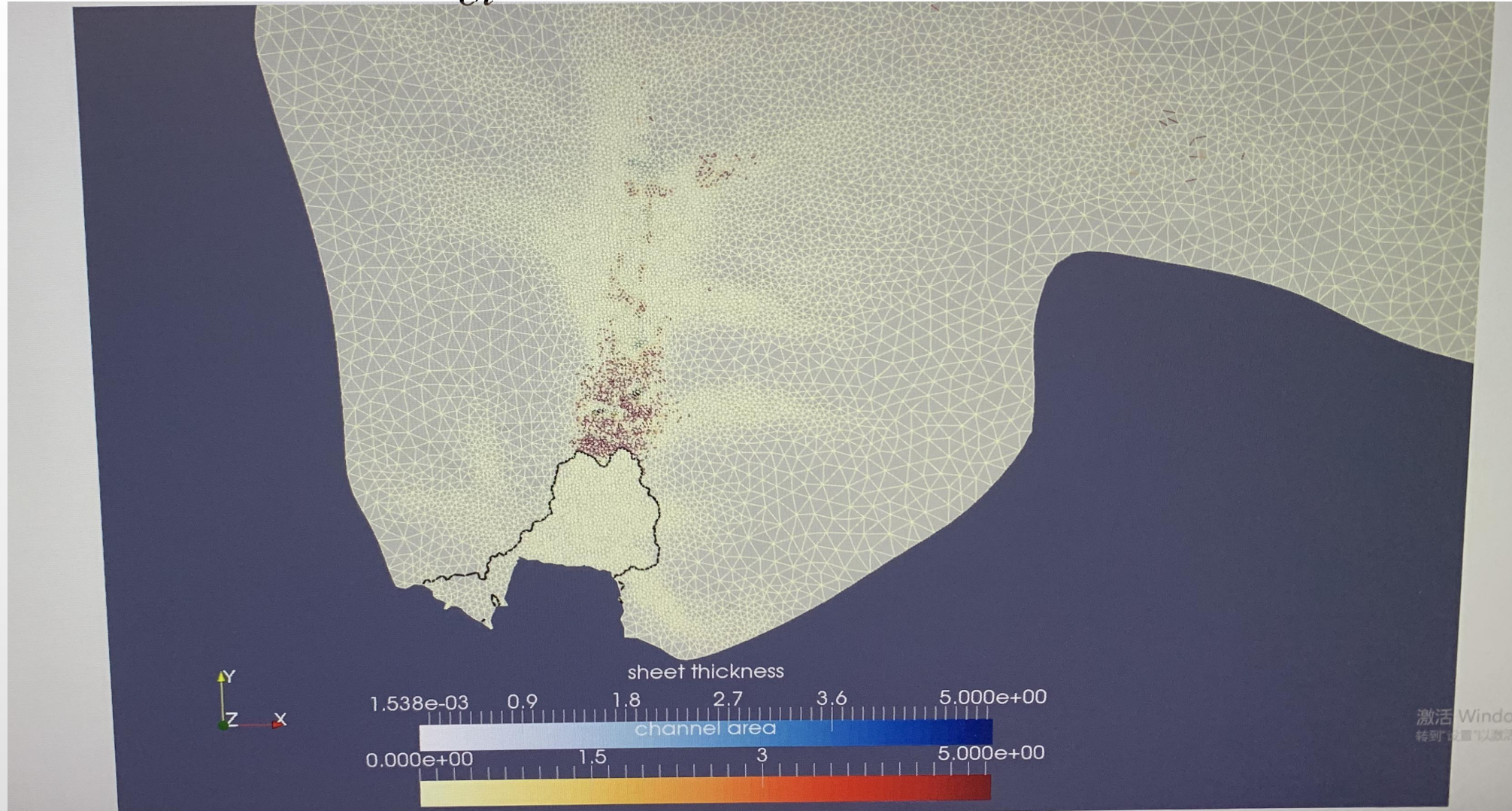
sticky points where shear heating accumulates.

Results

Sheet thickness
channel evolving

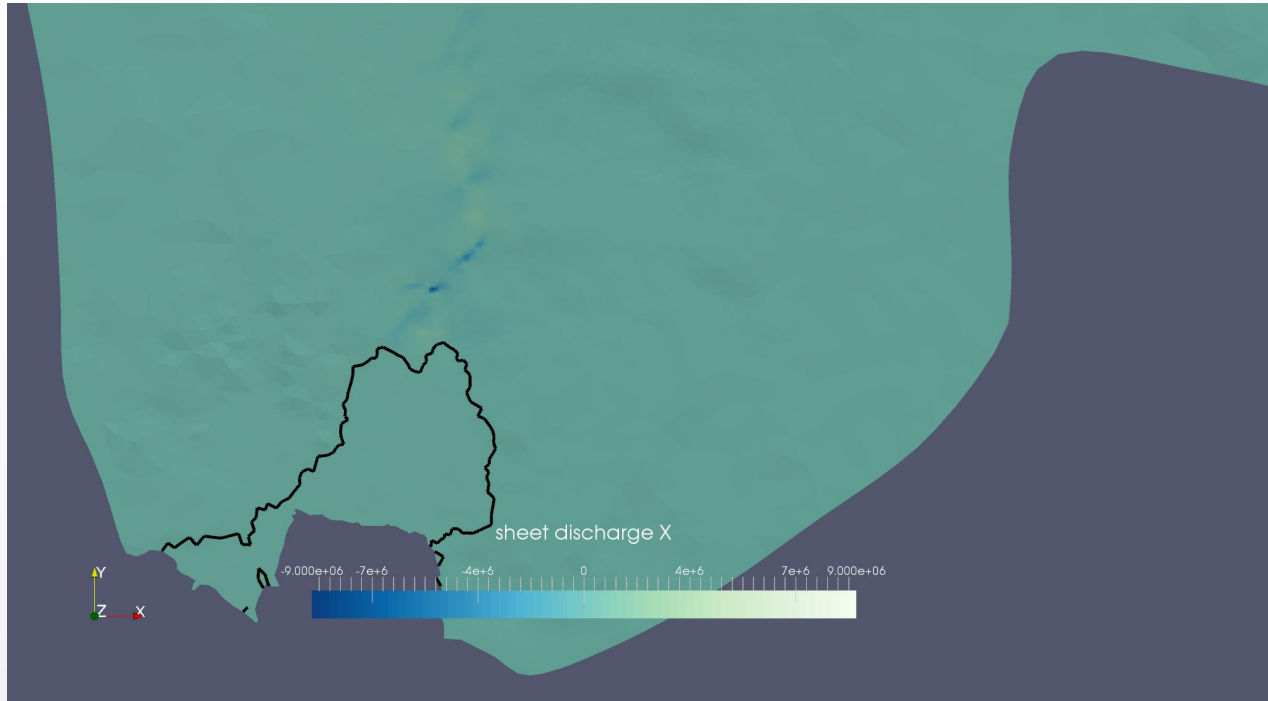
h [0.001,0.1] m
 S [0,5] m²

$$\frac{\partial h}{\partial t} = w - v$$
$$\frac{\partial h}{\partial t} + \nabla q = m$$

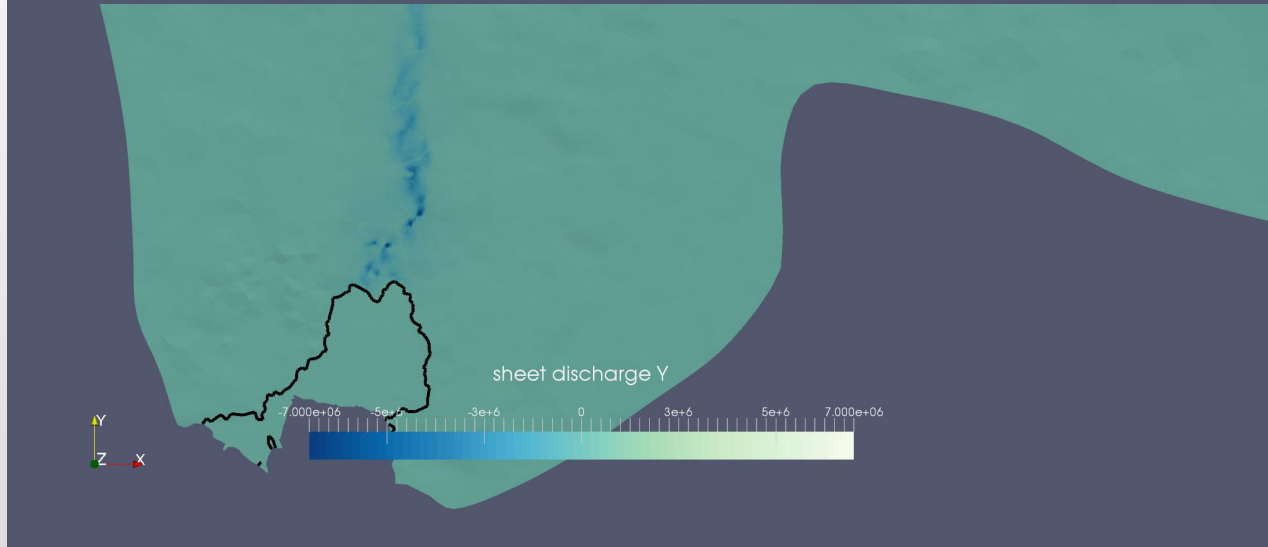


Results
800days

qx



qy



$$q = -\kappa h^\alpha |\nabla \phi|^{\beta-2} \nabla \phi$$

$$\frac{\partial h}{\partial t} + \nabla q = m$$

- High water pressure consistent with more sheet discharge.

Outlook

- Need further realistic water input to drive Glads from inversion model
- Need more results analysis and sensitivity tests
- Couple model with ice dynamics, give more realistic and detailed results.
- Couple to ocean model to simulate ocean circulation.

Thank you!

Yufang Zhang

PhD student

Email: 201831490020@mail.bnu.edu.cn

Wechat: xiaoyzyf